

wNetKAT:
Programming and Verifying
Software-Defined Networks

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Computer Networks

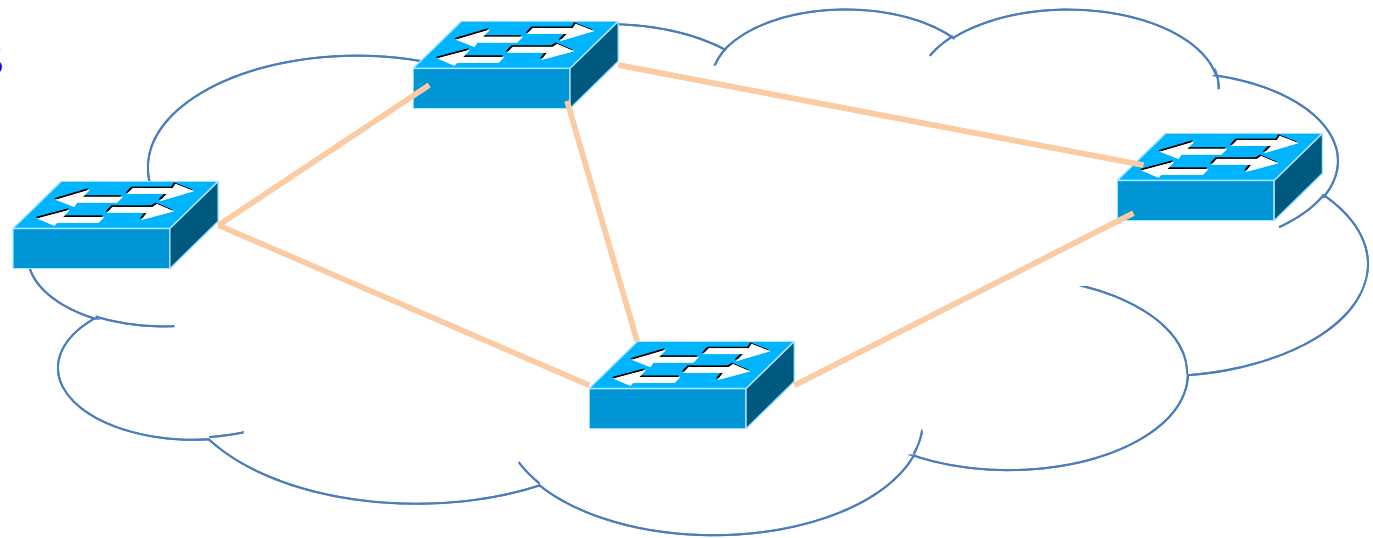
- Computer networks (datacenter networks, enterprise networks, wide-area networks) have become a **critical infrastructure** of the information society
- For the future:
dependable and flexible enough?

Traditional Networks

Traditional Networks: Data Plane

Data plane:
Packet streaming

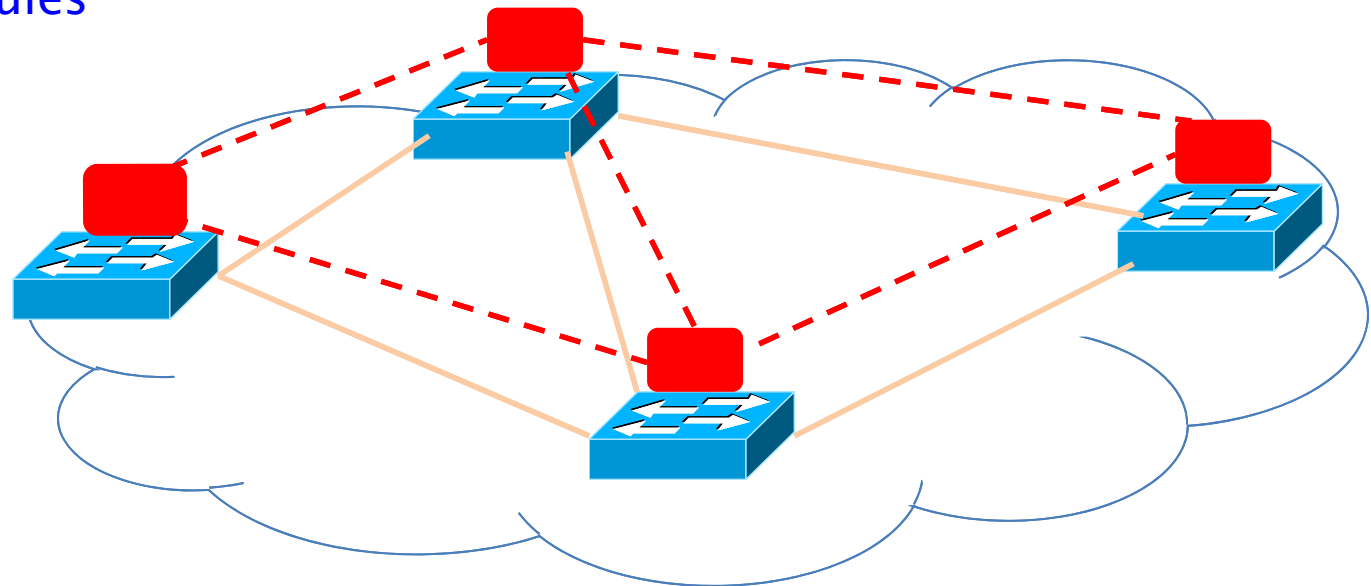
Forward
Filter
Buffer
Mark
Rate-limit
Measure packets



Traditional Networks: (Distributed) Control Plane

Control plane:
Distributed algorithms

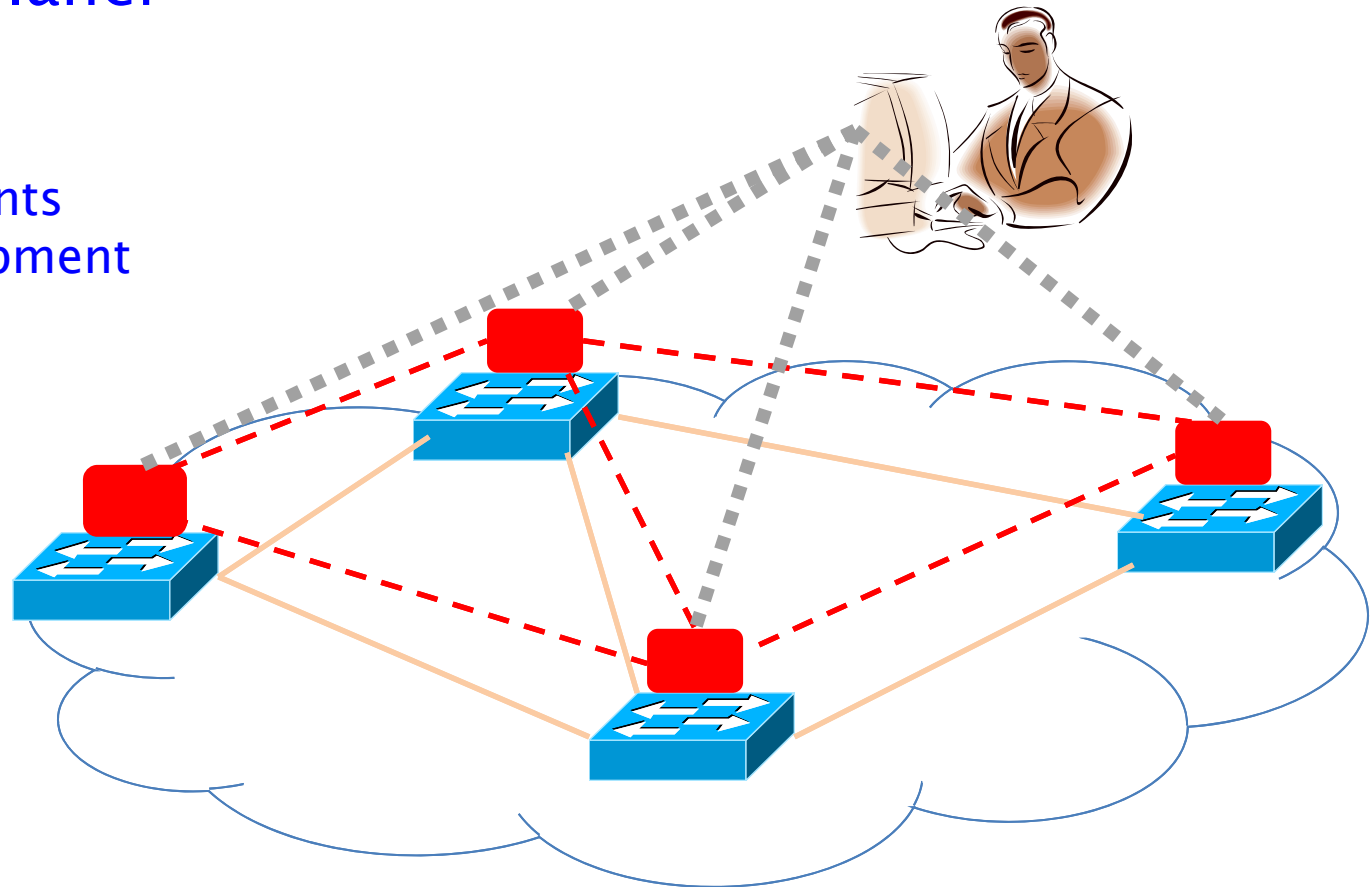
Track topology changes
Compute routes
Install forwarding rules



Traditional Networks: Management Plane

Management plane:
Humans

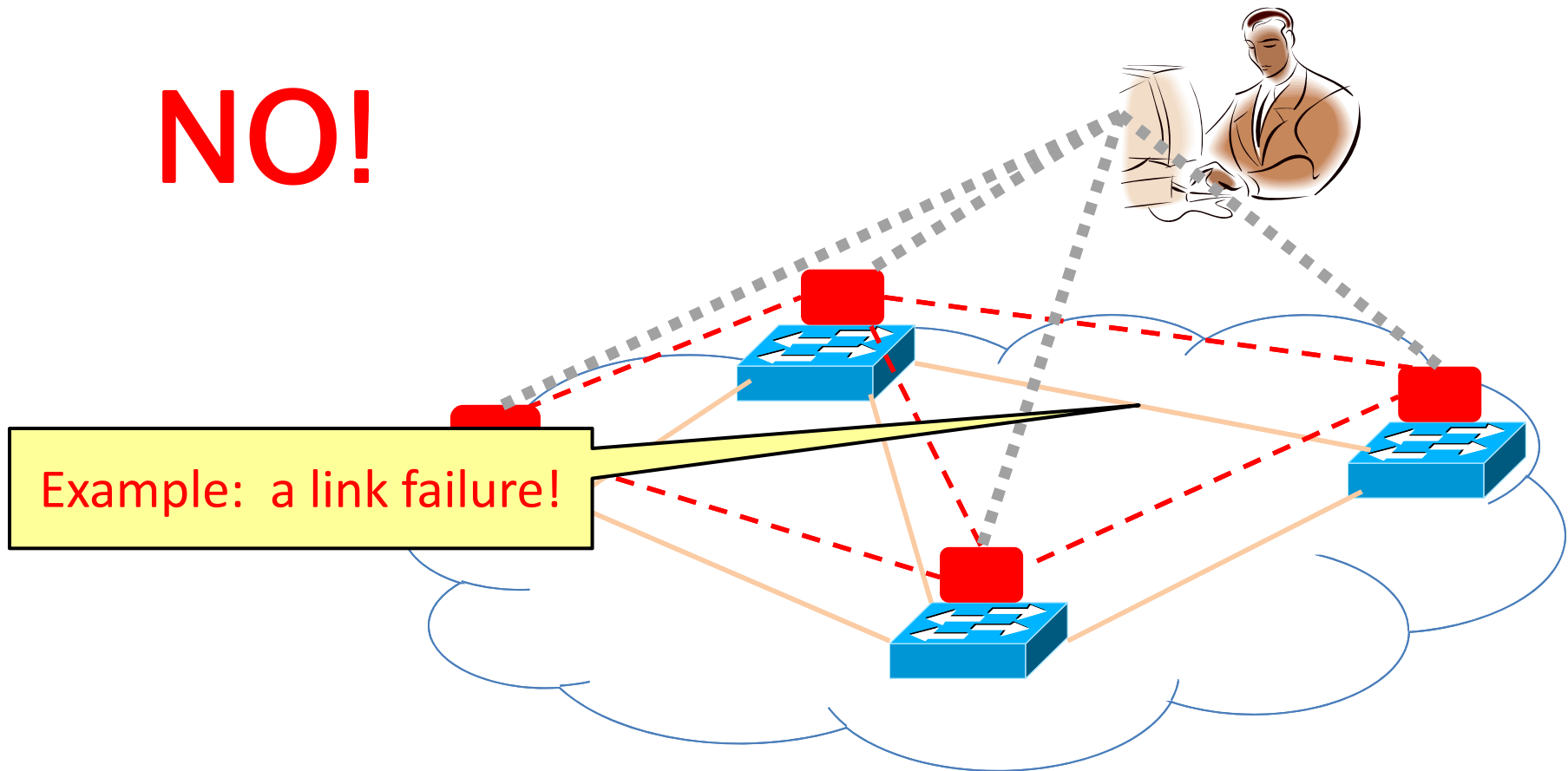
Collect measurements
Configure the equipment



Traditional Networks

- Dependable and flexible enough?

NO!

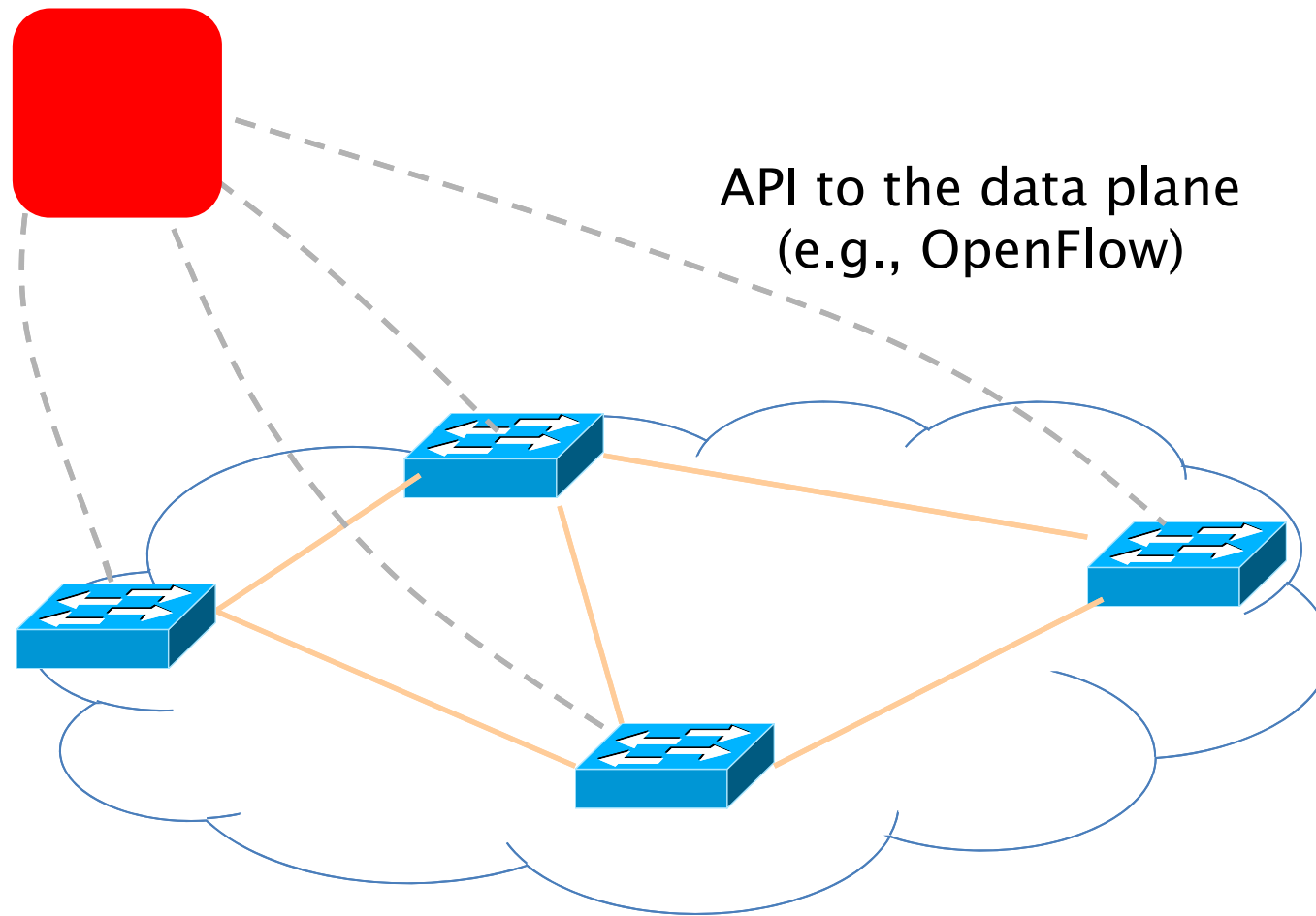


Solution: *Software-Defined Networks (SDN)*!

- “A Purpose-Built Global Network: Google’s Move to SDN”
 - One of the key reasons for Google’s move to SDN: **faster and more efficient**/fine-grained traffic engineering, improving WAN network utilization.
 - A second reason: **more predictable behavior** under failures (no unpredictable and slow distributed reconvergence).

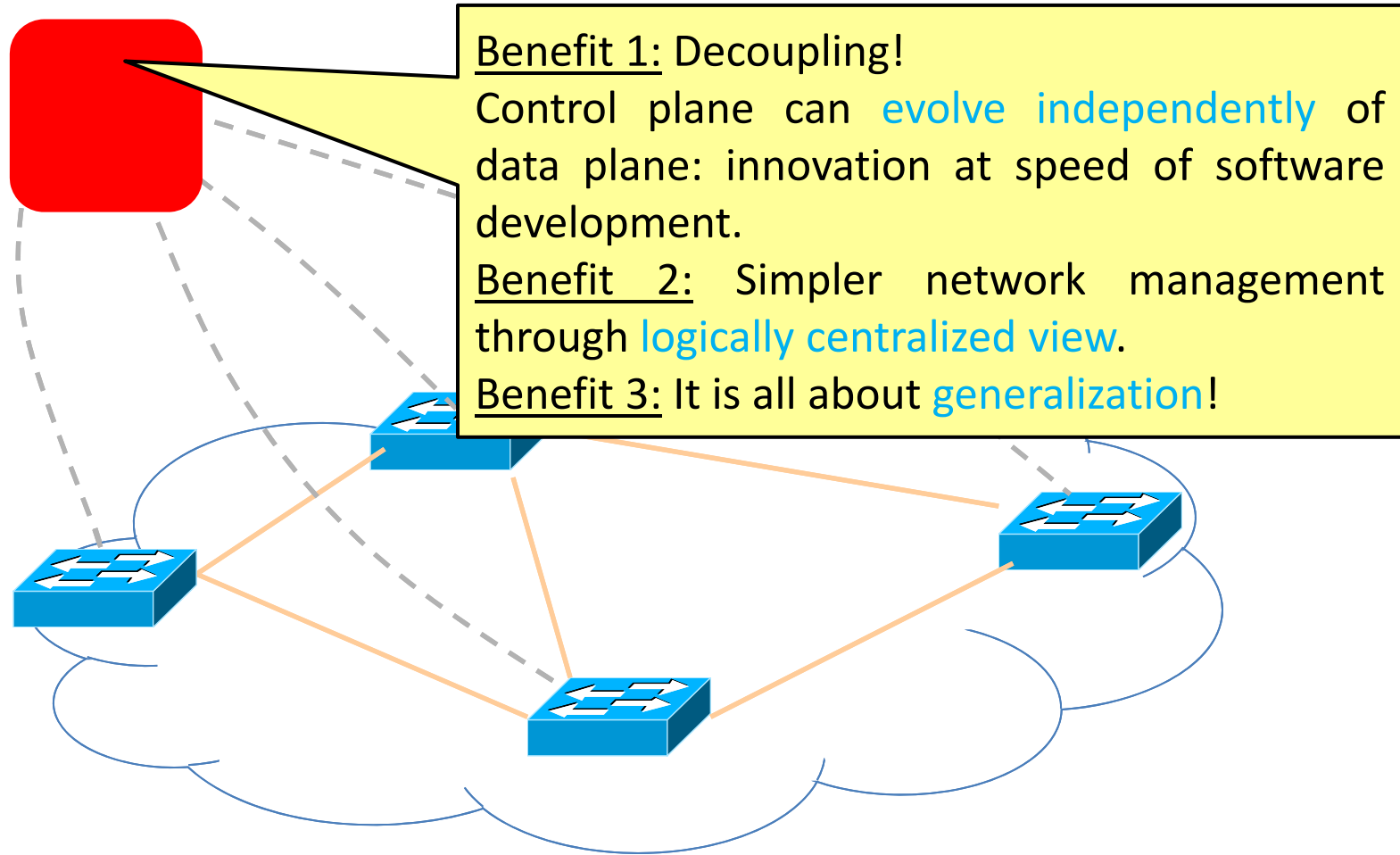
Software Defined Networks (SDN)

Logically-centralized controller

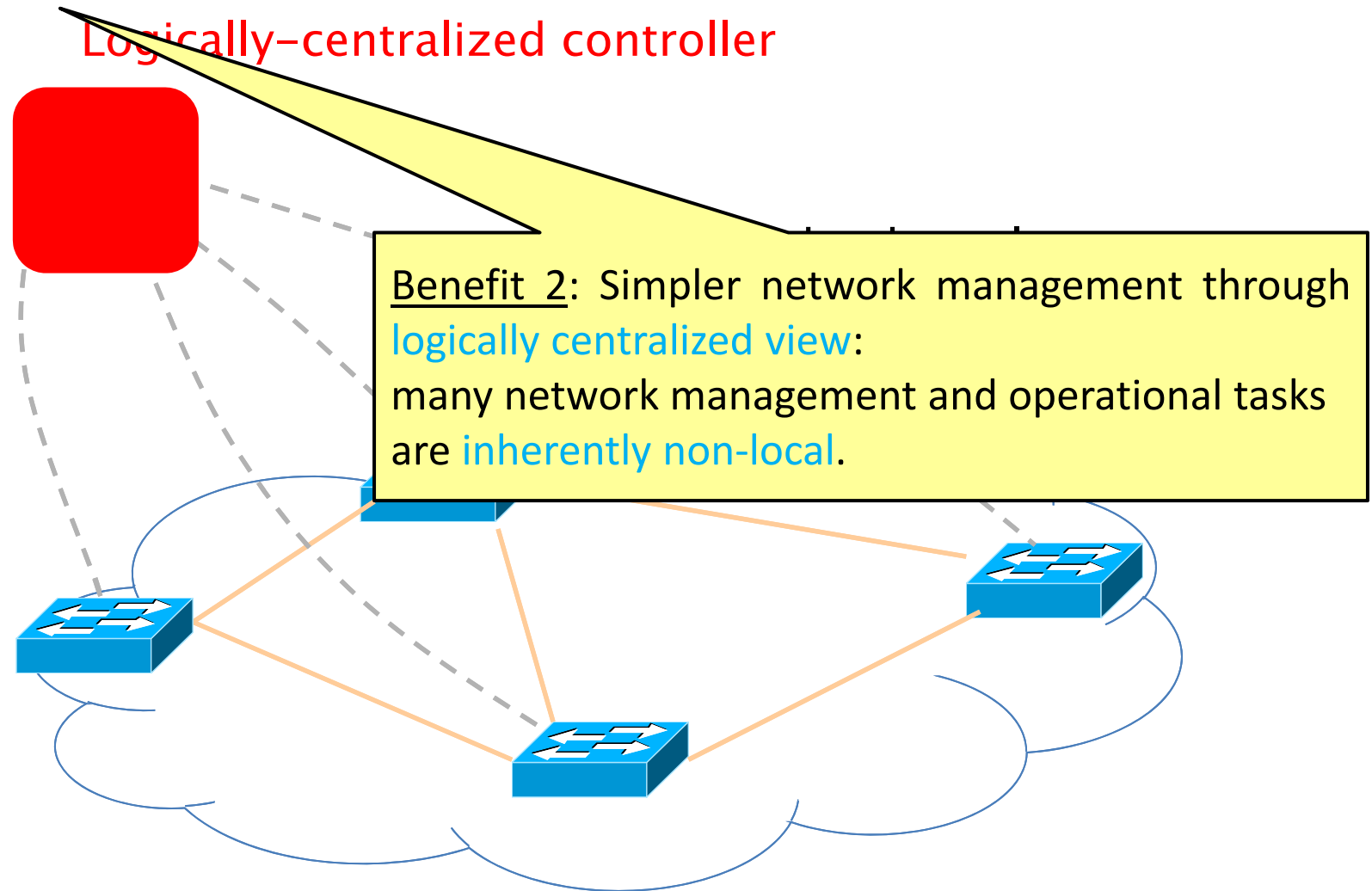


Software Defined Networks (SDN)

Logically-centralized controller



Software Defined Networks (SDN)



Software Defined Networks (SDN)

Logically-centralized controller

Benefit 3: OpenFlow is about **generalization!**

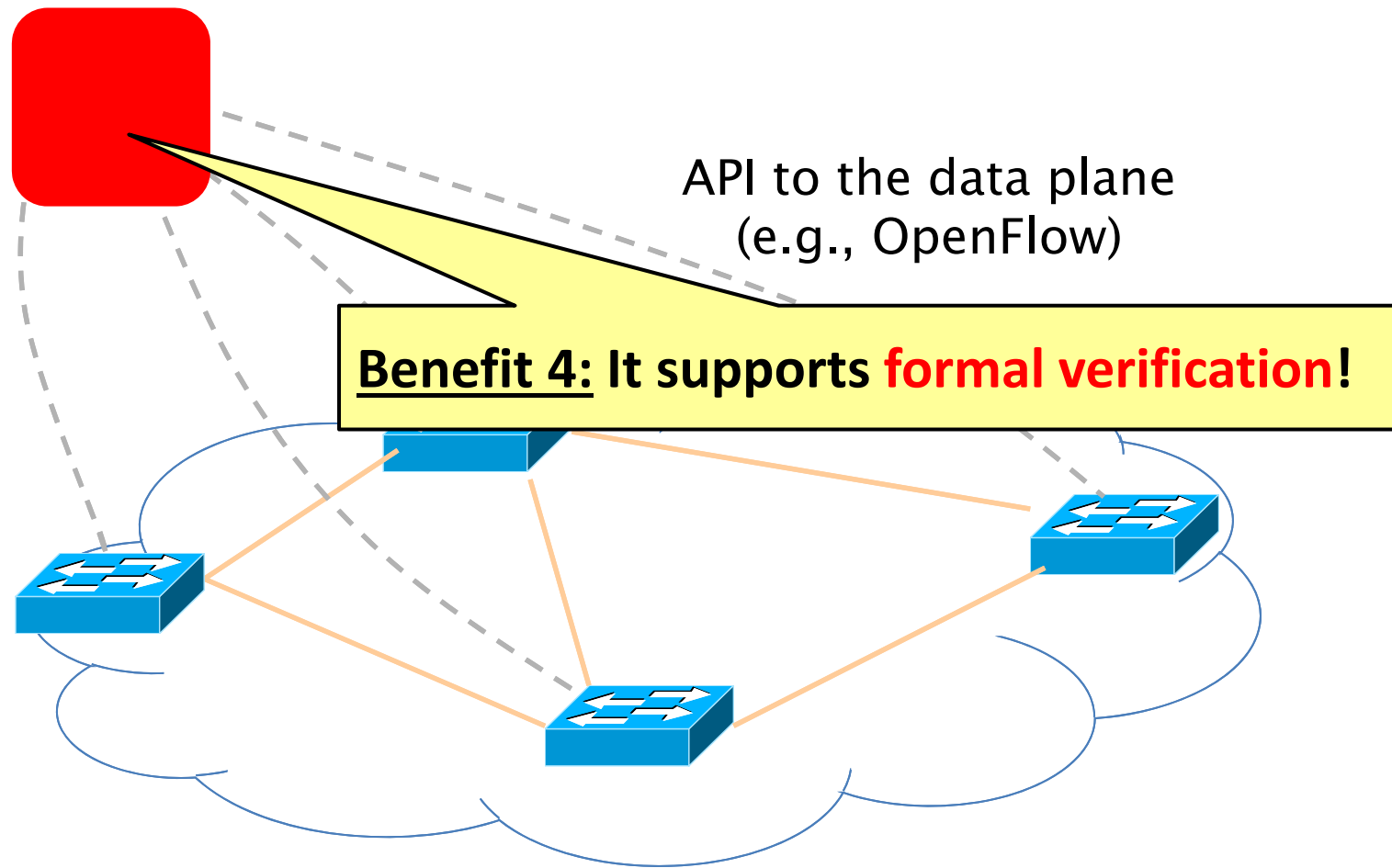
- Generalize devices (L2-L4: switches, routers, middleboxes)
- Generalize routing and traffic engineering (not only destination-based)
- Generalize flow-installation: coarse-grained rules and wildcards okay, proactive vs reactive installation
- Provide general and logical network views to the application / tenant

to the data plane
e.g., OpenFlow)



Software Defined Networks (SDN)

Logically-centralized controller

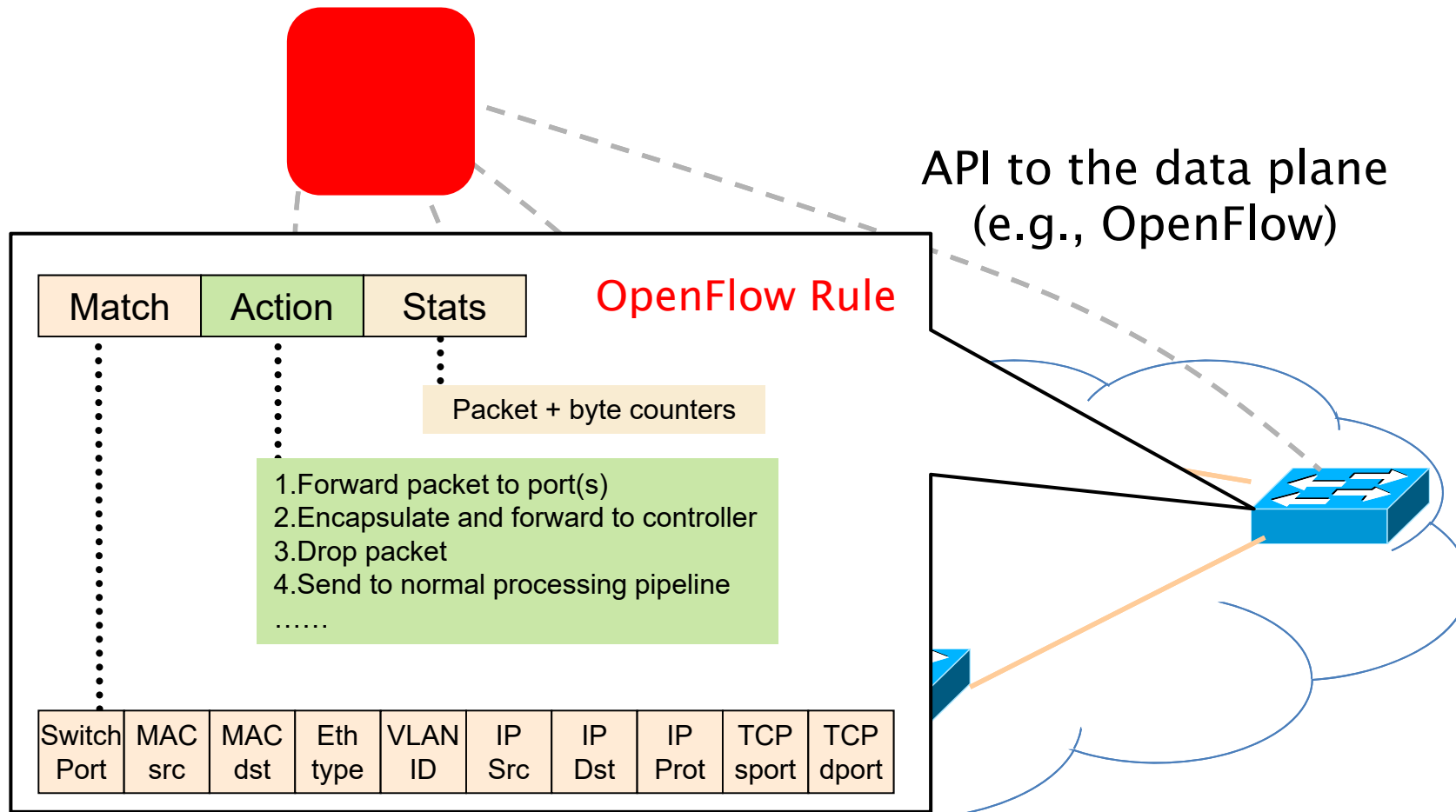


Programming SDN

- Programming languages for networks lie at the heart of SDN

Programming SDN

Logically-centralized controller



Programming SDN

- Programming languages for networks lie at the heart of SDN
- OpenFlow is very **low-level**: inconvenient for programmers
- Researchers have started developing more high-level languages
- **NetKAT**: state-of-the-art framework for programming and reasoning about networks

NetKAT

- Kleene Algebra (KA) $(K, +, \cdot, *, 0, 1)$
 - $+, \cdot$ binary operators
 - $*$ unary operator
 - $0, 1$ constants
- KAT $(K, B, +, \cdot, *, \bar{}, 0, 1)$, $B \subseteq K$
 - $(K, +, \cdot, *, 0, 1)$ KA
 - $(B, +, \cdot, \bar{}, 0, 1)$ Boolean Algebra
 - $(B, +, \cdot, 0, 1)$ subalgebra of $(K, +, \cdot, 0, 1)$
- NetKAT: KAT with the following atoms
 - $f \leftarrow w$ assignment
 - $f = w$ test
 - ***dup*** duplication

NetKAT

Syntax

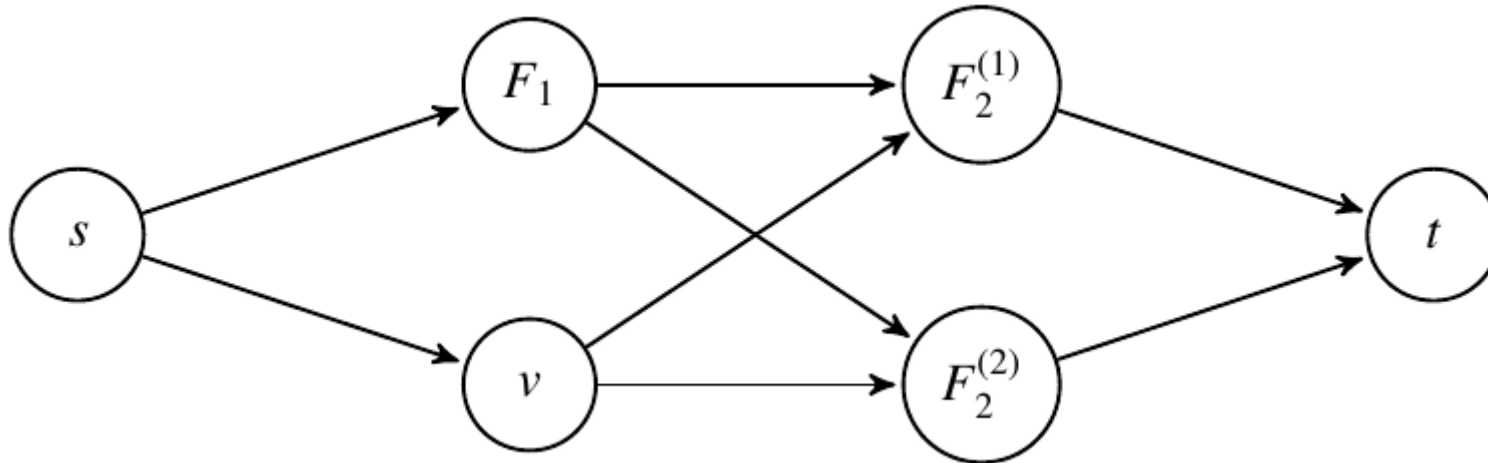
Fields	$f ::= f_1 \mid \cdots \mid f_k$	
Packets	$pk ::= \{f_1 = v_1, \dots, f_k = v_k\}$	
Histories	$h ::= pk::\langle \rangle \mid pk::h$	
Predicates	$a, b ::= 1$	<i>Identity</i>
	0	<i>Drop</i>
	$f = n$	<i>Test</i>
	$a + b$	<i>Disjunction</i>
	$a \cdot b$	<i>Conjunction</i>
	$\neg a$	<i>Negation</i>
Policies	$p, q ::= a$	<i>Filter</i>
	$f \leftarrow n$	<i>Modification</i>
	$p + q$	<i>Union</i>
	$p \cdot q$	<i>Sequential composition</i>
	p^*	<i>Kleene star</i>
	dup	<i>Duplication</i>

Semantics

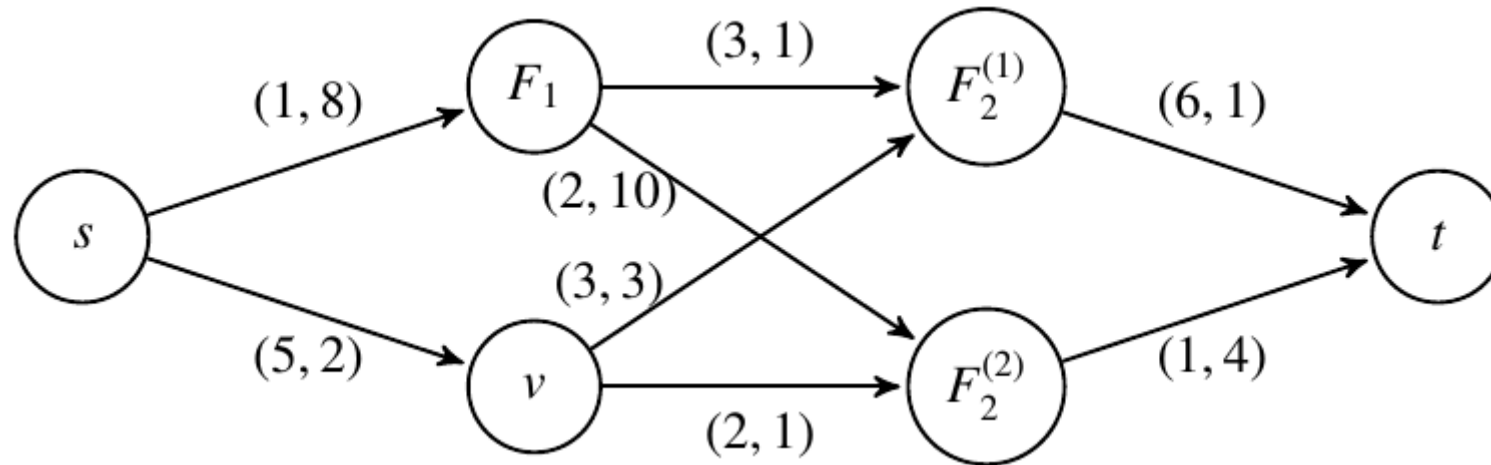
	$\llbracket p \rrbracket \in \mathbf{H} \rightarrow \mathcal{P}(\mathbf{H})$
	$\llbracket 1 \rrbracket h \triangleq \{h\}$
	$\llbracket 0 \rrbracket h \triangleq \{\}$
	$\llbracket f = n \rrbracket (pk::h) \triangleq \begin{cases} \{pk::h\} & \text{if } pk.f = n \\ \{\} & \text{otherwise} \end{cases}$
	$\llbracket \neg a \rrbracket h \triangleq \{h\} \setminus (\llbracket a \rrbracket h)$
	$\llbracket f \leftarrow n \rrbracket (pk::h) \triangleq \{pk[f := n]::h\}$
	$\llbracket p + q \rrbracket h \triangleq \llbracket p \rrbracket h \cup \llbracket q \rrbracket h$
	$\llbracket p \cdot q \rrbracket h \triangleq (\llbracket p \rrbracket \bullet \llbracket q \rrbracket) h$
	$\llbracket p^* \rrbracket h \triangleq \bigcup_{i \in \mathbb{N}} F^i h$
	where $F^0 h \triangleq \{h\}$ and $F^{i+1} h \triangleq (\llbracket p \rrbracket \bullet F^i) h$
	$\llbracket \text{dup} \rrbracket (pk::h) \triangleq \{pk::(pk::h)\}$

‘;’ instead of ‘.’ in policies!

NetKAT: Example


$$\begin{aligned} t \quad ::= & \quad sw = s; (sw \leftarrow F_1 + sw \leftarrow v) \\ & + sw = F_1; (sw \leftarrow F_2^{(1)} + sw \leftarrow F_2^{(2)}) \\ & + sw = v; (sw \leftarrow F_1^{(1)} + sw \leftarrow F_2^{(2)}) \\ & + sw = F_2^{(1)}; sw \leftarrow t \\ & + sw = F_2^{(2)}; sw \leftarrow t \end{aligned}$$

NetKAT: Example



Weighted NetKAT!

wNetKAT

- Add quantitative variables!
- Add switch variables (quantitative, non-quantitative)
- Quantitative Assignment

$$x \leftarrow (\sum_{x' \in \mathcal{V}'} x' + \delta)$$

- Quantitative Test

$$x \bowtie (\sum_{x' \in \mathcal{V}'} x' + \delta)$$

where: $x \in \mathcal{V}_q$, $\mathcal{V}' \subseteq \mathcal{V}_q$, $\bowtie \in \{>, <, \geq, \leq, =\}$, $\delta \in \mathbb{N}$ (or \mathbb{Q})

x might be from \mathcal{V}'

\mathcal{V}_q (\mathcal{V}_n) can be either packet or switch!

& instead of NetKAT +

wNetKAT

$$\llbracket x \leftarrow \omega \rrbracket(\rho, pk :: h) = \begin{cases} \{\rho, pk[\omega/x] :: h\} & \text{if } x \in \mathcal{V}_p \\ \{\rho(v)[\omega/x], pk :: h\} & \text{if } x \in \mathcal{V}_s \text{ and } pk(sw) = v \end{cases}$$

$$\llbracket x = \omega \rrbracket(\rho, pk :: h) = \begin{cases} \{\rho, pk :: h\} & \text{if } x \in \mathcal{V}_p \text{ and } pk(x) = \omega \\ & \text{or if } x \in \mathcal{V}_s, pk(sw) = v \text{ and } \rho(v, x) = \omega \\ \emptyset & \text{otherwise} \end{cases}$$

$$\llbracket y \leftarrow (\sum_{y' \in \mathcal{V}} y' + r) \rrbracket(\rho, pk :: h) = \begin{cases} \{\rho, pk[r'/x] :: h\} & \text{if } x \in \mathcal{V}_p \\ \{\rho(v)[r'/x], pk :: h\} & \text{if } x \in \mathcal{V}_s \text{ and } pk(sw) = v \end{cases}$$

where $r' = \sum_{y_p \in \mathcal{V}' \cap \mathcal{V}_p} pk(y_p) + \sum_{y_s \in \mathcal{V}' \cap \mathcal{V}_q} \rho(v, y_s) + r$

$$\llbracket y = (\sum_{y' \in \mathcal{V}} y' + r) \rrbracket(\rho, pk :: h) = \begin{cases} \{\rho, pk :: h\} & \text{if } x \in \mathcal{V}_p \text{ and } pk(x) = r' \\ & \text{or } x \in \mathcal{V}_s, pk(sw) = v \text{ and } \rho(v, x) = r' \\ \emptyset & \text{otherwise} \end{cases}$$

where $r' = \sum_{y_p \in \mathcal{V}' \cap \mathcal{V}_p} pk(y_p) + \sum_{y_s \in \mathcal{V}' \cap \mathcal{V}_q} \rho(v, y_s) + r$

$$x \in \mathcal{V}_n, y \in \mathcal{V}_q$$

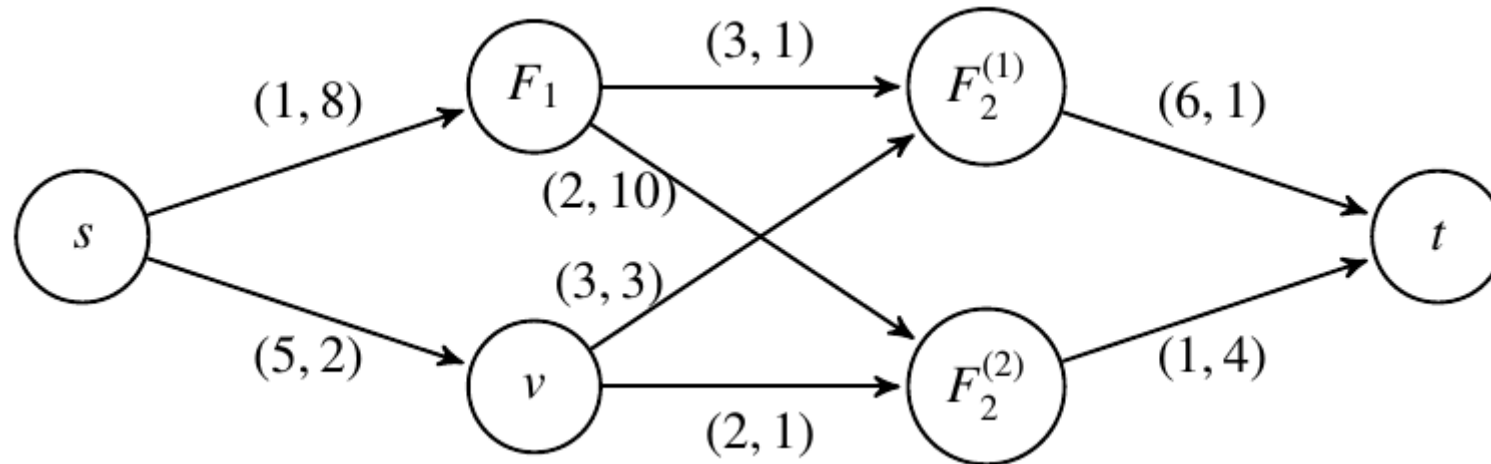
wNetKAT

- Other arithmetic operations

- min or max can be easily defined:

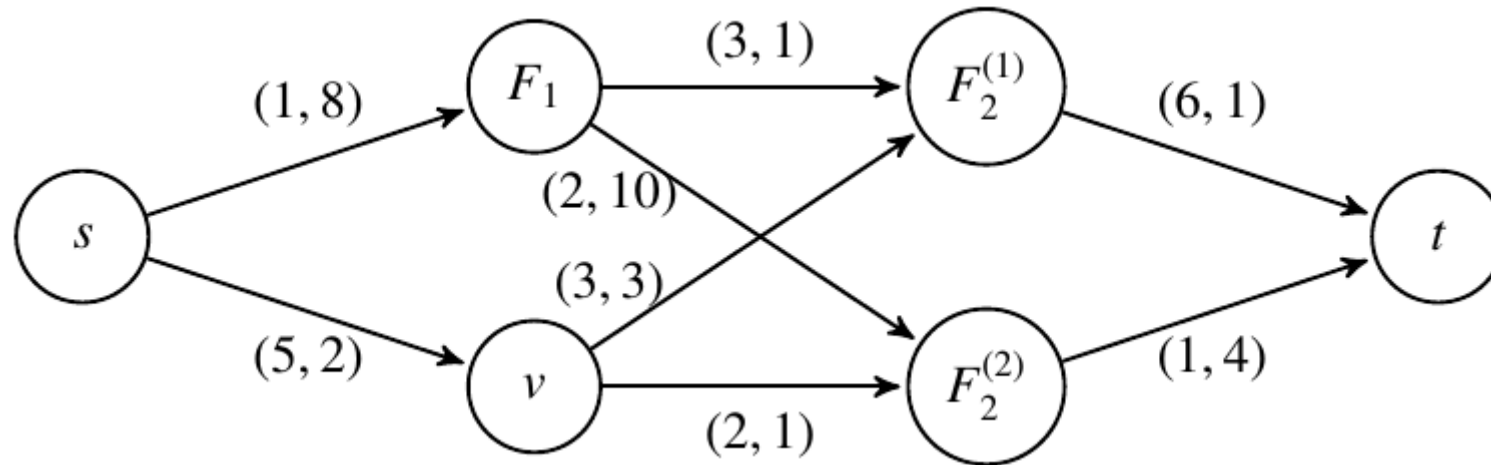
$$x \leftarrow \min\{y, z\} \stackrel{\text{def}}{=} y \leq z; x \leftarrow y \& y > z; x \leftarrow z.$$

Example



$$\begin{aligned}
 t ::= & \text{ } sw = s; (sw \leftarrow F_1; co \leftarrow co + 1; ca \leftarrow \min\{ca, 8\} \\
 & \quad \& \text{ } sw \leftarrow v; co \leftarrow co + 5; ca \leftarrow \min\{ca, 2\}) \\
 & \& \text{ } sw = F_1; \\
 & \quad (sw \leftarrow F_2^{(1)}; co \leftarrow co + 3; ca \leftarrow \min\{ca, 1\} \\
 & \quad \& \text{ } sw \leftarrow F_2^{(2)}; co \leftarrow co + 2; ca \leftarrow \min\{ca, 10\}) \\
 & \& \text{ } sw = v; (sw \leftarrow F_2^{(1)}; co \leftarrow co + 3; ca \leftarrow \min\{ca, 3\} \\
 & \quad \& \text{ } sw \leftarrow F_2^{(2)}; co \leftarrow co + 2; ca \leftarrow \min\{ca, 1\}) \\
 & \& \text{ } sw = F_2^{(1)}; sw \leftarrow t; co \leftarrow co + 6; ca \leftarrow \min\{ca, 1\} \\
 & \& \text{ } sw = F_2^{(2)}; sw \leftarrow t; co \leftarrow co + 1; ca \leftarrow \min\{ca, 4\}
 \end{aligned}$$

Example

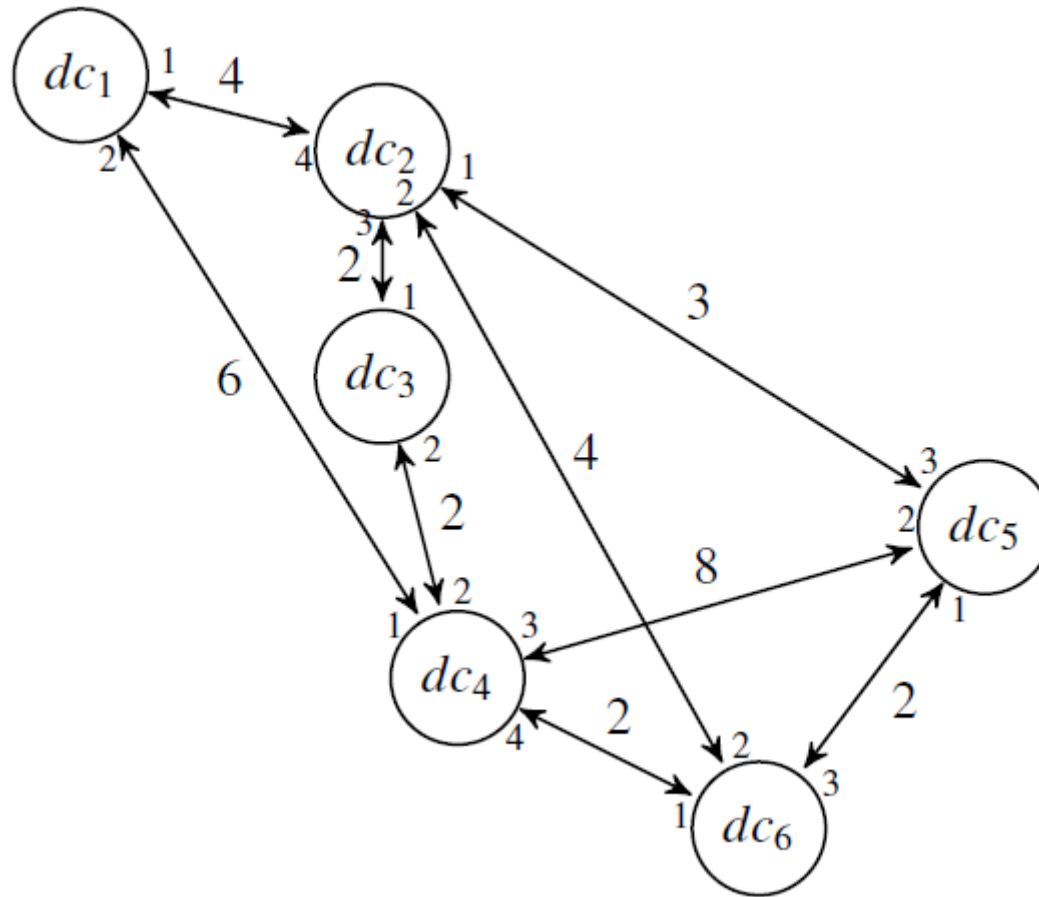


$$p_{F_2} ::= (sw = F_2^{(1)} \ \& \ sw = F_2^{(2)}); ca \leftarrow ca + \gamma$$

Only packet variables in this example

Applications: Cost Reachability

- “Can node B be reached from A at **cost at most c?**”



Applications: Cost Reachability

- “Can node B be reached from A at cost at most c ?”

- Topology ' t '

e.g., $dc_1 \rightarrow dc_2$

$sw = dc_1; pt = 1; sw \leftarrow dc_2; pt \leftarrow 4; l \leftarrow l + 4$

- Policy ' p '

e.g., dc_2

sr
 $(p$

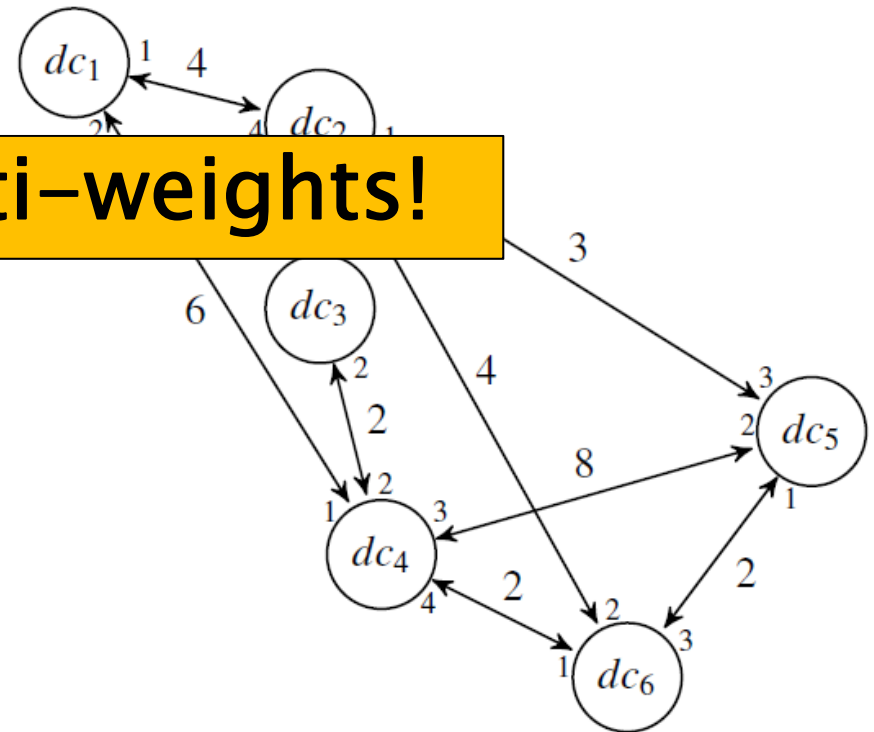
Also works for multi-weights!

- Check whether the following equal to "drop"

$scr \leftarrow A; dst \leftarrow B; l \leftarrow 0; sw \leftarrow A;$

$pt(pt)^*;$

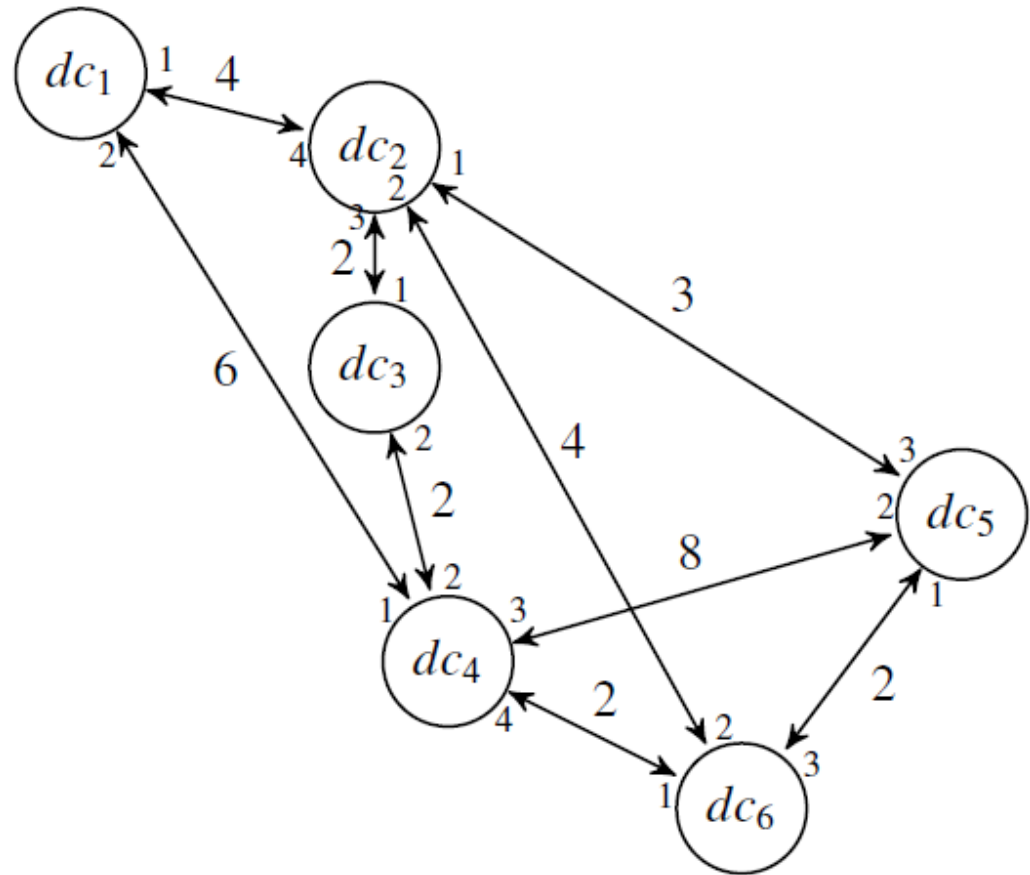
$sw = B; l \leq c.$



Applications: Capacitated Reachability

- “Can node A communicate with B at **rate at least r** ?”

- Unsplittable
- Splittable



Applications: Capacitated Reachability

- “Can node A communicate with B at rate at least r ?”

- Unsplittable

- Topology ' t '

e.g., $dc_1 \rightarrow dc_2$

$sw = dc_1; pt = 1;$

$sw \leftarrow dc_2; pt \leftarrow 4; c \leftarrow \min\{c, 4\}$

- Policy ' p '

e.g., dc_2

$src = dc_1; dst = dc_5; sw = dc_2; pt = 4;$

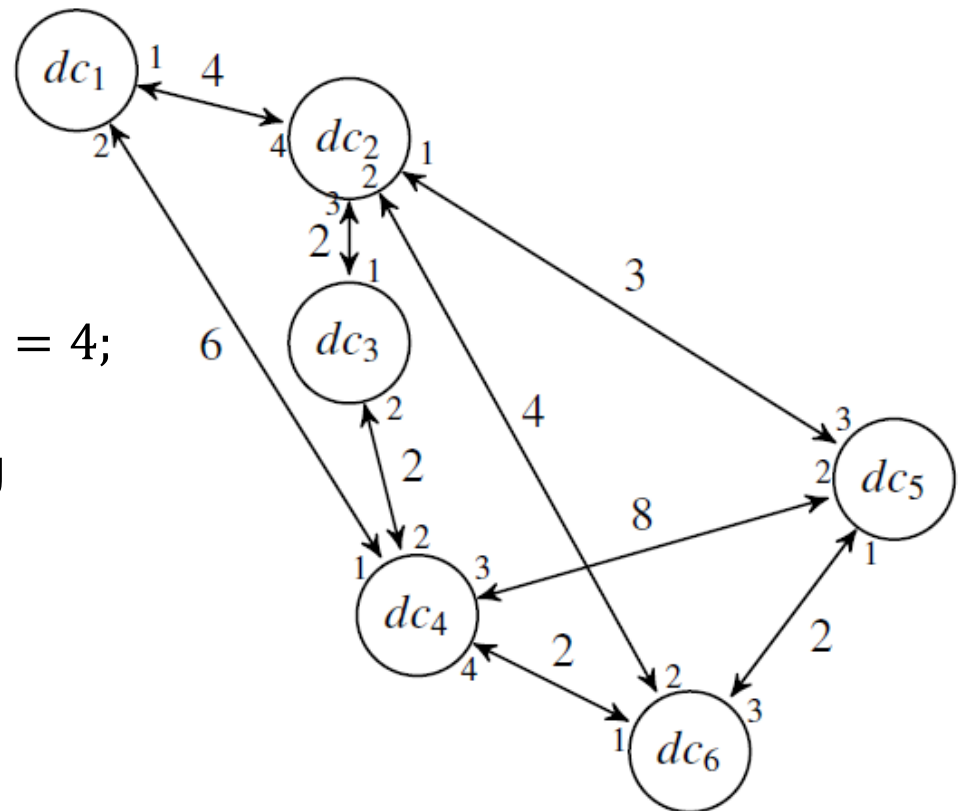
$(pt \leftarrow 1 \ \& \ pt \leftarrow 3)$

- Check whether the following equal to "drop"

$scr \leftarrow A; dst \leftarrow B; c \leftarrow r; sw \leftarrow A;$

$pt(pt)^*;$

$sw = B; c \geq r.$



Applications: Capacitated Reachability

- “Can node A communicate with B at rate at least r ?”

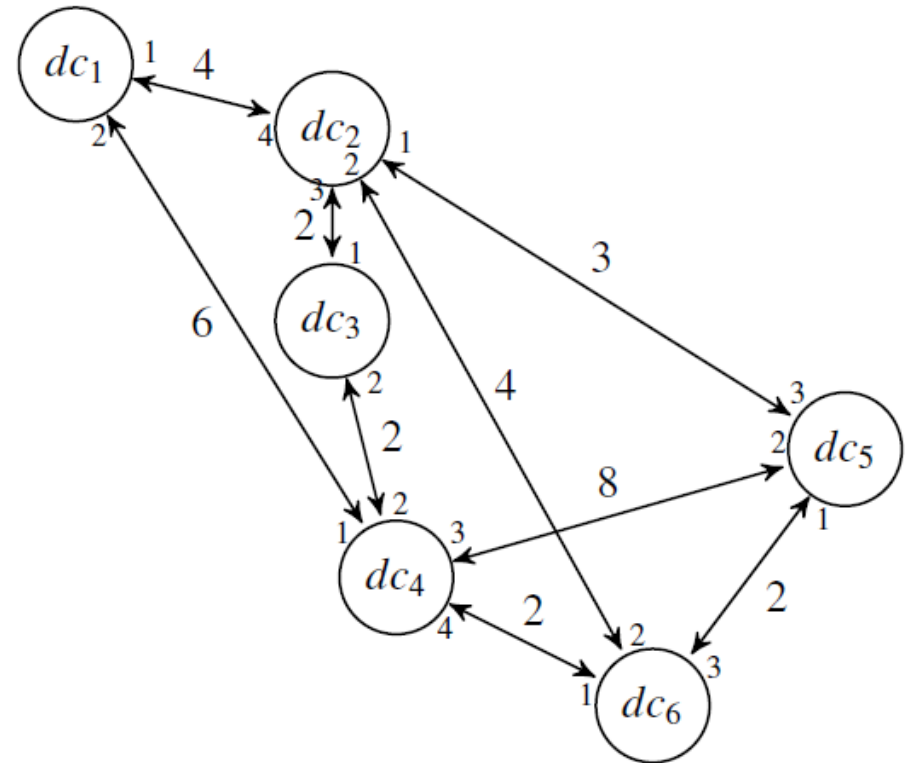
- **Splittable**

- Topology ' t '

e.g., $dc_1 \rightarrow dc_2$

$sw = dc_1; pt = 1;$

$sw \leftarrow dc_2; pt \leftarrow 4; c \leftarrow \min\{c, 4\}$



Applications: Capacitated Reachability

- “Can node A communicate with B at rate at least r ?”

- Splittable

- Policy ' p '

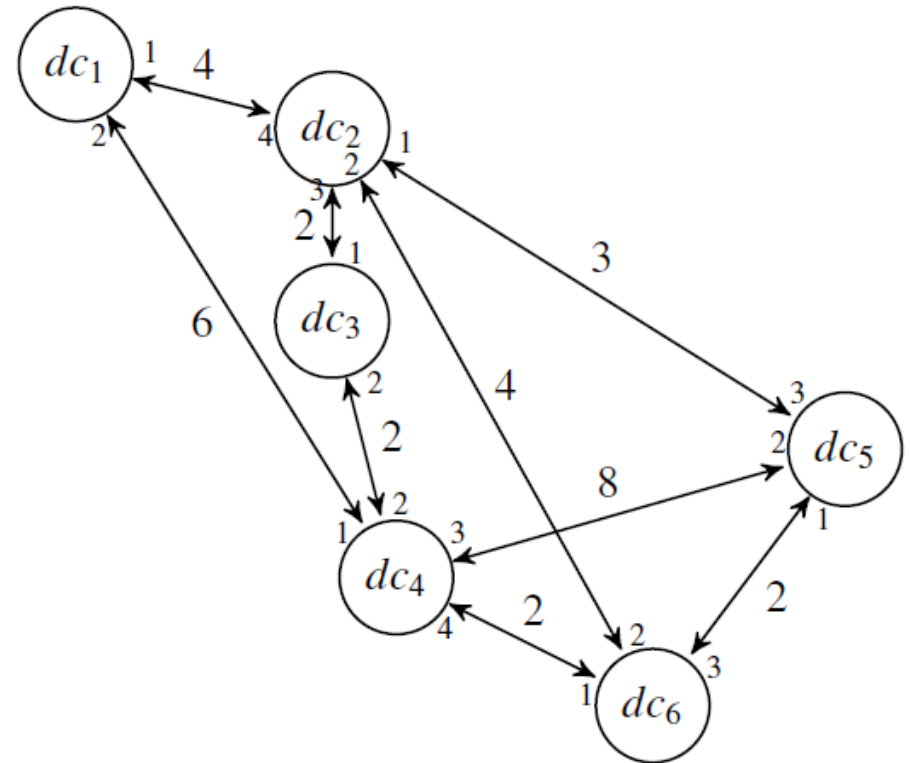
- Split: e.g., dc_2

$src = dc_1; dst = dc_5; sw = dc_2;$

$pt = 4; c \leq 5;$

$((pt \leftarrow 1; c \leftarrow \min\{c, 3\})$

$\& (pt \leftarrow 3; c \leftarrow \max\{0, c - 3\}))$



Applications: Capacitated Reachability

- “Can node A communicate with B at rate at least r ?”

- Splittable

- Policy ' p '

- Split

- Merge: e.g., dc_4

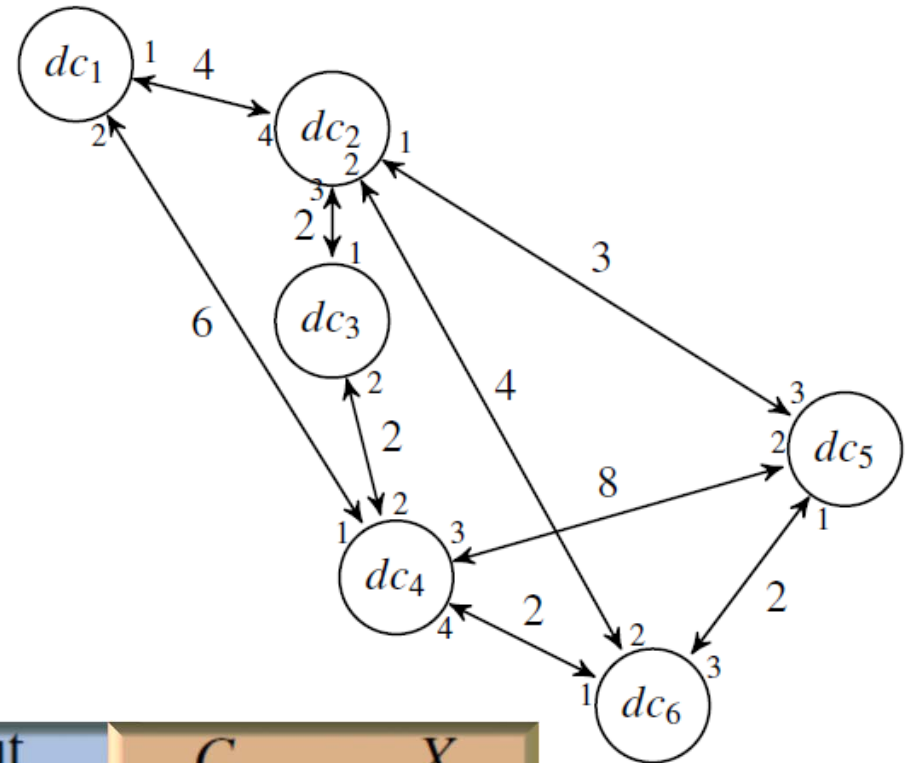
$sw = dc_4; src = dc_1; dst = dc_5;$

$(pt = 1 \ \& \ pt = 2);$

$C = C + c; X \leftarrow X - 1;$

$(X \neq 0; drop$

$\& X = 0; c \leftarrow C; pt \leftarrow 3).$



src	dst	in	out	C	X
dc_1	dc_5	1, 2	3	0	2
dc_5	dc_2	3, 4	1, 2	0	2

Applications: Capacitated Reachability

- “Can node A communicate with B at rate at least r ?”
- Splittable

- Policy ' p '

$sw = dc_4; src = dc_5; dst = dc_2;$

$(pt = 3 \ \& \ pt = 4);$

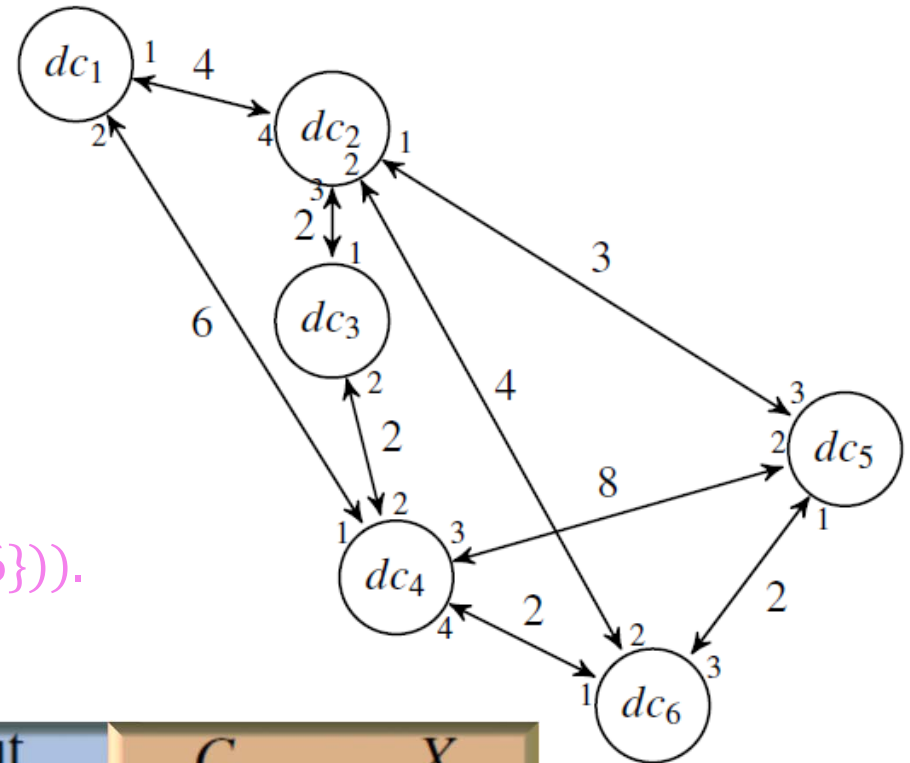
$C = C + c; X \leftarrow X - 1;$

$(X \neq 0; drop$

$\& X = 0; c \leftarrow C; c \leq 8$

$((pt \leftarrow 1; c \leftarrow \min\{6, c\})$

$\& (pt \leftarrow 2; c \leftarrow \max\{0, c - 6\})).$



src	dst	in	out	C	X
dc_1	dc_5	1, 2	3	0	2
dc_5	dc_2	3, 4	1, 2	0	2

Applications: Capacitated Reachability

- “Can node A communicate with B at rate at least r ?”

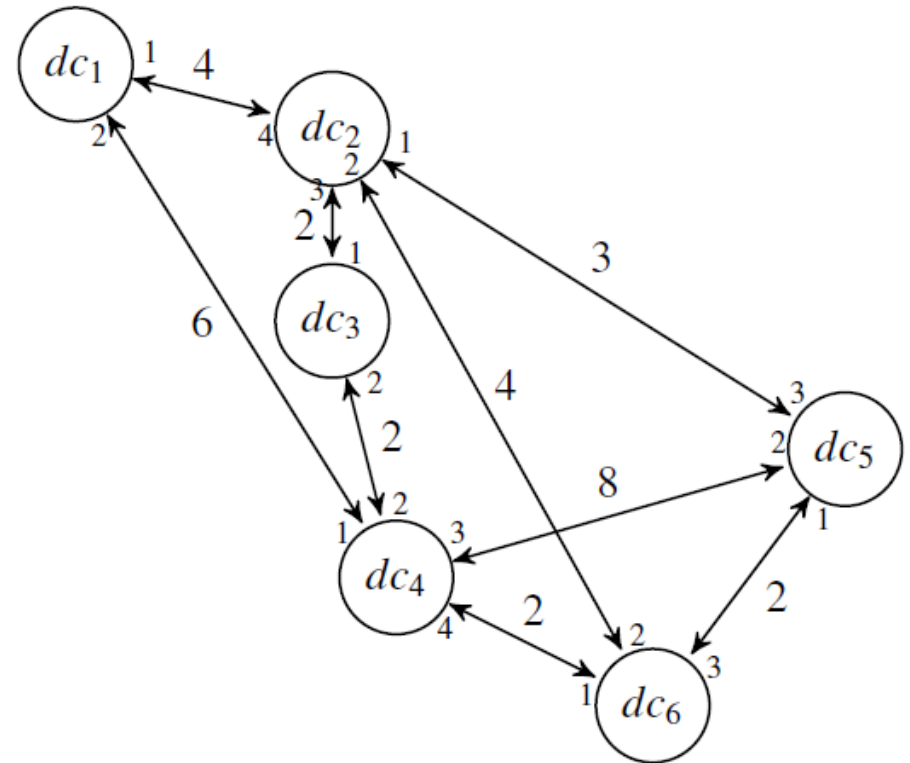
- **Splittable**

- Check whether the following equal to "drop"

$scr \leftarrow A; dst \leftarrow B; c \leftarrow r; sw \leftarrow A;$

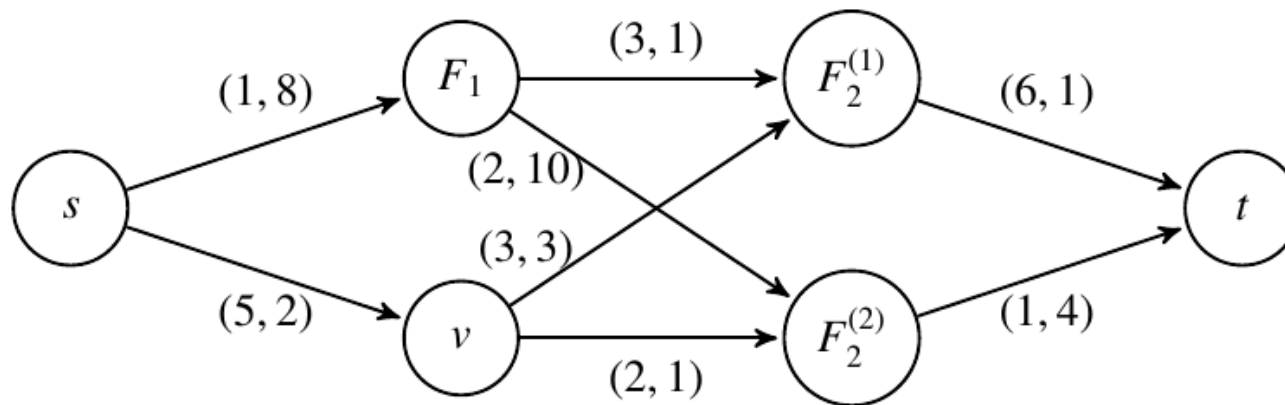
$pt(pt)^*;$

$sw = B; c \geq r.$



Applications: Service Chain

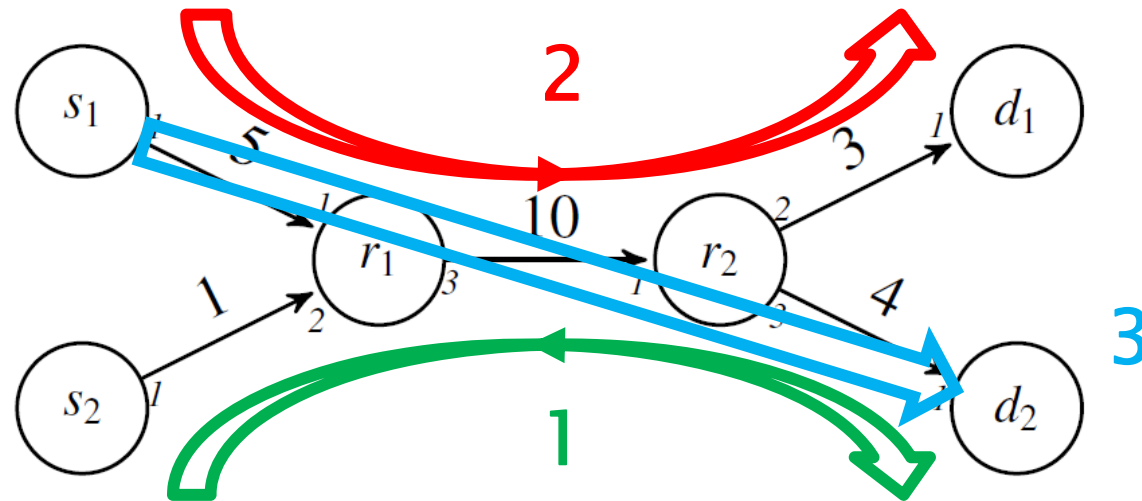
- “Can node A reach B at cost/latency at most l and/or at rate/bandwidth at least r , via the **service chain**?”



- Check whether the following equal to "drop"
 $src \leftarrow s; dst \leftarrow t; co \leftarrow 0; ca \leftarrow r; sw \leftarrow s;$
 $pt(pt)^*;$
 $sw = F_1; p_{F_1}; t(pt)^*; sw = F_2; p_{F_2}; t(pt)^*;$
 $sw = t; co \leq l; ca \geq r.$

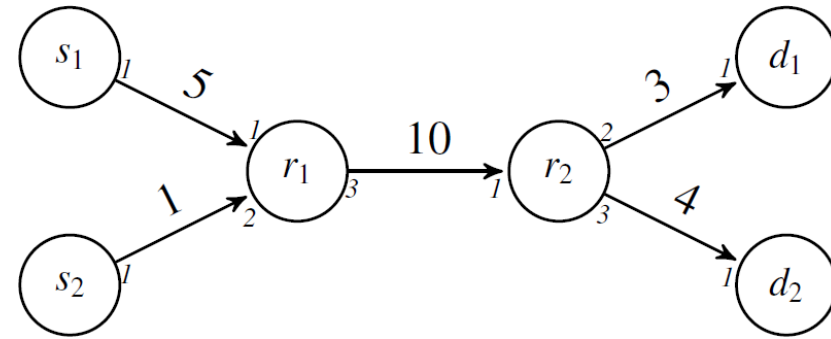
Applications: Fairness

- “Does the current flow allocation satisfy **max-min fairness** requirements?”



Applications: Fairness

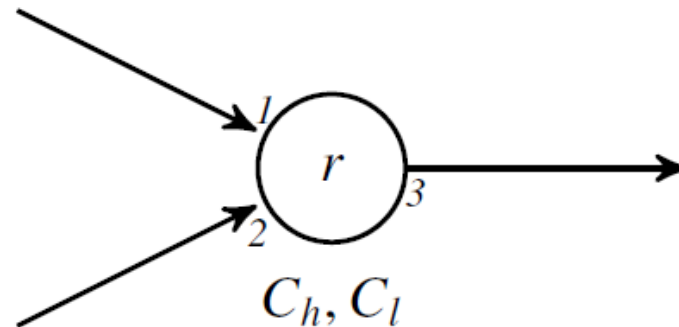
- “Does the current flow allocation satisfy **max-min fairness** requirements?”



$$\begin{aligned}
 f_3 &= sw \leftarrow s_2; scr \leftarrow s_2; dst \leftarrow d_2; a \leftarrow 10; \\
 &x_3 \leftarrow 1; x_1 \leftarrow 0; x_2 \leftarrow 0; tp(tp)^*; sw = d_2; x_3 = a \\
 f_1 &= sw \leftarrow s_1; scr \leftarrow s_1; dst \leftarrow d_1; a \leftarrow 10; \\
 &x_1 \leftarrow 2; x_3 \leftarrow 1; x_2 \leftarrow 0; tp(tp)^*; sw = d_1; x_1 = a \\
 f_2 &= sw \leftarrow s_1; scr \leftarrow s_1; dst \leftarrow d_2; a \leftarrow 10; \\
 &x_2 \leftarrow 3; x_1 \leftarrow 2; x_3 \leftarrow 1; tp(tp)^*; sw = d_1; x_2 = a
 \end{aligned}$$

Applications: Quality of Service

- E.g., prioritize a certain flow (e.g., a VoIP call) over another (e.g., a Dropbox synchronization).



$sw = r; (pt = 1 \ \& \ pt = 2);$

$(x = high; C_h < 8; pt \leftarrow 3; C_h \leftarrow C_h + 1;$

$\& \ x = low; C_l < 2; pt \leftarrow 3; C_l \leftarrow C_l + 1);$

$C_h = 8; C_l = 2; C_h \leftarrow 0; C_l \leftarrow 0$

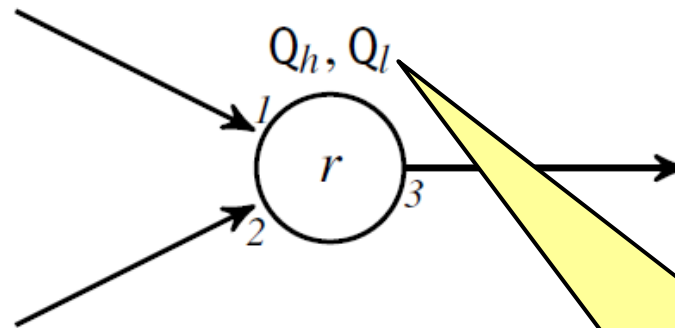
Further Extension: Queues

$$\llbracket \text{EQ } Q \rrbracket(\rho, pk :: h) = \begin{cases} \llbracket 1^* \rrbracket(\rho, pk :: h) & \text{if } Q \neq \text{FULL}, \\ & \text{then } EQ(Q) \\ \emptyset & \text{otherwise} \end{cases}$$

$$\llbracket \text{DQ } Q \rrbracket(\rho, pk :: h) = \begin{cases} \{\rho, pk :: h\} & \text{if } \text{HEAD}(Q) = pk :: h \\ & \text{then } DQ(Q) \\ \llbracket 1^* \rrbracket(\rho, pk :: h) & \text{otherwise} \end{cases}$$

Applications: Quality of Service

- E.g., prioritize a certain flow (e.g., a VoIP call) over another (e.g., a Dropbox synchronization).



$sw = r; x = low; EQ Q_l \& sw =$

$sw = r; x = high;$

$(x_h < 8; DQ Q_h; pt \leftarrow 3; x_h \leftarrow x_h + 1$

$\& x_h = 8; Q_l = \emptyset; DQ Q_h; pt \leftarrow 3$

$\& x_h = 8; Q_l \neq \emptyset; skip)$

$x_h = 8; x_l = 2; x_h \leftarrow 0; x_l \leftarrow 0$

Coming soon!

(Un)Decidability

- Theorem: (undecidability)

Deciding equivalence of two WNetKAT expressions is equal to deciding the equivalence of the two corresponding weighted WNetKAT automata.

- Theorem:

Deciding whether a WNetKAT expression is equal to “*drop*” is equal to deciding the emptiness of the corresponding weighted automaton.

Questions?

Thank you
for your attention!